

Gr 9 Wiskunde: Inhoudsarea 2

Patrone, Algebra & Grafieke

ANTWOORDE

- Patrone
- Algebraïese Uitdrukkinge
- Faktorisering
- Algebraïese Vergelykinge
- Grafieke



PATRONE

1.1 C < ... 1^2 ; 3^2 ; 5^2 ; **7^2**

1.2 C < ... 18 ; 36 ; **54** ; 72 ; **90**

1.3 A < ... $\frac{1}{2^0}$; $\frac{1}{2^1}$; $\frac{1}{2^2}$; **$\frac{1}{2^3}$** ; $\frac{1}{2^4}$

1.4 A < ... $\frac{1}{3}$; **$\frac{1}{6}$** ; $\frac{1}{12}$; $\frac{1}{24}$; $\frac{1}{48}$

1.5 D < ... 1^2+2 ; 2^2+2 ; 3^2+2 ; 4^2+2 ; **5^2+2**



2.1 a) $T_n = 3n$:
 3 ; 6 ; 9 < ... $3(1)$; $3(2)$; $3(3)$

b) $T_n = 5n$:
 5 ; 10 ; 15 < ... $5(1)$; $5(2)$; $5(3)$

c) $T_n = 3n + 1$:
 4 ; 7 ; 10 < ... $3(1) + 1$; $3(2) + 1$; $3(3) + 1$

d) $T_n = 5n - 2$:
 3 ; 8 ; 13 < ... $5(1) - 2$; $5(2) - 2$; $5(3) - 2$

e) $T_n = n^2$:
 1 ; 4 ; 9 < ... $(1)^2$; $(2)^2$; $(3)^2$

f) $T_n = n^3$:
 1 ; 8 ; 27 < ... $(1)^3$; $(2)^3$; $(3)^3$

2.2 a) $T_{12} = 3(12) = 36$ <

b) $T_{12} = 5(12) = 60$ <

c) $T_{12} = 3(12) + 1 = 37$ <

d) $T_{12} = 5(12) - 2 = 58$ <

e) $T_{12} = (12)^2 = 144$ <

f) $T_{12} = (12)^3 = 1728$ <



3.1 $y = 3x$ <

3.2 $a = 7$ < ... $7 \times 3 = 21$

$b = 30$ < ... $10 \times 3 = 30$

4.1 Die konstante verskil = **7** <

4.2 3 ; 10 ; 17 ; 24 ; 31 ; **38** ; **45** <

4.3 Die konstante **verskil** is **7** ... sien Vraag 4.1

Skryf dus **die veelvoude van 7** neer ... waar $T_n = 7n$:

7 ; 14 ; 21 ; 28 ; 35 ; ...

en vergelyk die gegewe ry:

3 ; 10 ; 17 ; 24 ; 31 ; ...

Elke term is **4 minder** as die veelvoude van 7 .

$\therefore T_n = 7n - 4$ <

Posisie in patroon	1	2	3	4	5
Term	1	8	27	64	125

5.2 $T_n = n^3$ <

5.3 As $T_n = 512$, dan is **$n = 8$** <

$$\left(\begin{array}{l} \dots 512 = 2^9 \\ = 2^3 \times 2^3 \times 2^3 \\ = 8 \times 8 \times 8 \\ = 8^3 < \end{array} \right. \left. \begin{array}{l} 2 \overline{)512} \\ 2 \overline{)256} \\ 2 \overline{)128} \\ 2 \overline{)64} \\ 2 \overline{)32} \\ 2 \overline{)16} \\ 2 \overline{)8} \\ 2 \overline{)4} \\ 2 \end{array} \right)$$

6.1 7 ; 11 ; 15 ; **19** ; **23** <

6.2 Die algemene **verskil** is **4**

Vergelyk dus die **veelvoude van 4** ... waar $T_n = 4n$:

4 ; 8 ; 12 ; 16 ; ...

met die gegewe ry:

7 ; 11 ; 15 ; 19 ; ...

Elke term is **3 meer** as die veelvoude van 4 .

$$\therefore T_n = 4n + 3 < \dots 7; 11; 15; 19; 23$$

6.3 $T_{50} = 4(50) + 3$
 $= 203$ <

7.1 3 ; 8 ; 13 ; **18** ; **23** <

7.2 Elke term is 5 meer as die vorige term <

7.3 Vergelyk $T_n = 5n$: 5 ; 10 ; 15 ; ...
to : 3 ; 8 ; 13 ; ...

Elke term is **2 minder** as die veelvoude van 5

$$\therefore T_n = 5n - 2 <$$



7.4 38 is 2 minder as 40 ; $40 = 5 \times 8$

$\therefore$ 38 is die **8^{ste}** term <

OF: Los die vergelyking op:

$$5n - 2 = 38 \quad \dots \text{die } n^{\text{de}} \text{ term} = 38$$

$$\text{Tel 2 by: } \therefore 5n = 40$$

$$\text{Deel deur 5: } n = 8$$

$\therefore$ Die **8^{ste}** term <

8.1	Figuur	1	2	3	4
	Aantal sye	5	9	13	17

<

8.2 Elke figuur het vier meer sye as die vorige figuur <

8.3 $T_n = 4n + 1$ < ... 5 ; 9 ; 13 ; 17
& elke term is **1 meer**
as die veelvoude van 4

9.	Figuur	1	2	3
	Aantal vuurhoutjies	6	9	12

9.1 Aantal vuurhoutjies in Figuur 4 = **15** <

9.2 $T_n = 3n + 3$ < ... 6 ; 9 ; 12
& elke term is **3 meer**
as die veelvoude van 3

$$9.3 \quad T_{20} = 3(20) + 3 \\ = 63 \text{ vuurhoutjies} <$$

10.1	Figuur	1	2	3	4
	Aantal swart teëls	1	2	3	4
	Aantal wit teëls	6	10	14	18

<

10.2 $T_n = 4n + 2$ < ... 6 ; 10 ; 14 ; 18
& elke term is **2 meer**
as die veelvoude van 4

11. Kyk na die patroon wat gevorm word deur die eerste getalle van elke reël:

1 ; 4 ; 9 ; ... die vierkante!
↑ ↑ ↑
ry 1 ry 2 ry 3
(1²) (2²) (3²)

$\therefore$ Die eerste getal in die **20^{ste}** ry sal **20² = 400** wees <

NOTAS



ALGEBRAÏESE UITDRUKKINGS

Terminologie

1.1 $-8 \blacktriangleleft \dots -8x^2$

1.2 $-7 \blacktriangleleft \dots$ die term met geen veranderlike nie

1.3 $-8x^2 + 2x - 7 \blacktriangleleft$

1.4 $1 \blacktriangleleft \dots 2x^1$

1.5 $2x - 7 - 8x^2$

$$\begin{aligned} x = \frac{1}{2}: \quad & 2\left(\frac{1}{2}\right) - 7 - 8\left(\frac{1}{2}\right)^2 \\ &= \left(\frac{2}{1}\right)\left(\frac{1}{2}\right) - 7 - \left(\frac{8}{1}\right)\left(\frac{1}{4}\right) \\ &= 1 - 7 - 2 \\ &= -8 \blacktriangleleft \end{aligned}$$

2. B $\blacktriangleleft \dots$ x is deel van die breuk $\frac{x-y}{3}$, wat ook as

$$\frac{1}{3}(x-y) = \frac{1}{3}x - \frac{1}{3}y \text{ geskryf kan word.}$$

$$\therefore \text{Die koëffisiënt van } x \text{ is } \frac{1}{3}.$$

[Die twee veranderlikes is x en y .]

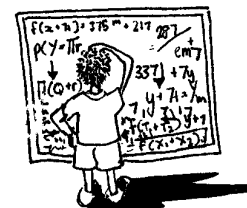
Substitusie

3.1 $2x^3 - 3x^2 + 9x + 2$
 $x = -2: \quad 2(-2)^3 - 3(-2)^2 + 9(-2) + 2$
 $= 2(-8) - 3(4) + 9(-2) + 2$
 $= -16 - 12 - 18 + 2$
 $= -44 \blacktriangleleft$

3.2 $y = 2x^2 - 3x + 5$
 $x = -1: \quad y = 2(-1)^2 - 3(-1) + 5$
 $= 2 + 3 + 5$
 $= 10 \blacktriangleleft$

3.3 $\frac{5ac}{b}$
 $= \frac{5\left(\frac{2}{1}\right)\left(\frac{1}{2}\right)}{(-3)} \dots$ wanneer mens met breuke werk, is dit nuttig om heelgetalle oor 1 te skryf.
 $= \frac{5(1)}{-3}$
 $= -\frac{5}{3} \blacktriangleleft$

3.4 $3x^2 - 2xy - y^2$
 $= 3(2)^2 - 2(2)(-3) - (-3)^2$
 $= 3(4) - 2(-6) - (9)$
 $= 12 + 12 - 9$
 $= 15 \blacktriangleleft$



Optel, Aftrek, Vermenigvuldig en Deel

4.1 $(2b - 3a - c) + (a - 4b + 2c)$ [OF: $-3a + 2b - c$
Tel op $\frac{a - 4b + 2c}{-2a - 2b + c} \blacktriangleleft$
 $= 2b - 3a - c + a - 4b + 2c$
 $= -3a + a + 2b - 4b - c + 2c$
 $= -2a - 2b + c \blacktriangleleft$

4.2 $-4x^2(5x^2 - 3x)$
 $= -20x^4 + 12x^3 \blacktriangleleft$



Distributiewe Eienskap:

$$a(b + c) = ab + ac$$



4.3 $\frac{8a + 16a^2 - 4a^3}{2a}$
 $= \frac{8a}{2a} + \frac{16a^2}{2a} - \frac{4a^3}{2a} \dots$ Elke **term** in die teller moet deur $2a$ gedeel word.
 $= 4 + 8a - 2a^2 \blacktriangleleft$

4.4 $-3(x)(x) + 2x(-x)$
 $= -3x^2 - 2x^2 \dots$ GELYKSOORTIGE TERME ☺
 $= -5x^2 \blacktriangleleft$

4.5 $-3m^2n(4m - 3mn^5 + 2n)$
 $= -12m^3n + 9m^3n^6 - 6m^2n^2 \blacktriangleleft \dots$ Distributiewe Eienskap

4.6 $3ab - (-2ab)$
 $= 3ab + 2ab \dots$ GELYKSOORTIGE TERME ☺
 $= 5ab \blacktriangleleft$

$$\begin{aligned} 5.1 \quad (3x)^3 + 2x^3 &= 27x^3 + 2x^3 \\ &= 29x^3 \quad \blacktriangleleft \end{aligned}$$

... $(3x)^3 = 3^3 \cdot x^3$
... GELYKSOORTIGE TERME ☺

$$\begin{aligned} 5.2 \quad (2x)^2 \times 3x^2 &= 4x^2 \times 3x^2 \\ &= 12x^4 \quad \blacktriangleleft \end{aligned}$$

... $(2x)^2 = 2x \times 2x$



$$\begin{aligned} 5.3 \quad (a^2b^3)^2 \cdot ab^2 &= a^4b^6 \cdot ab^2 \\ &= a^5b^8 \quad \blacktriangleleft \end{aligned}$$

$$\begin{aligned} 5.4 \quad 2^5 - 1^5 &= 32 - 1 \\ &= 31 \quad \blacktriangleleft \end{aligned}$$

... $2^5 = 2 \times 2 \times 2 \times 2 \times 2$
 $1^5 = 1 \times 1 \times 1 \times 1 \times 1$

Breuke (+, -, ×, ÷)

$$\begin{aligned} 5.5 \quad \frac{x \times 5}{2 \times 5} + \frac{x \times 2}{5 \times 2} &= \frac{5x + 2x}{10} \\ &= \frac{7x}{10} \quad \blacktriangleleft \end{aligned}$$

Wanneer ons breuke optel of aftrek, moet ons 'n gemene noemer bepaal.

$$\begin{aligned} 5.6 \quad \frac{5a \times 3}{8 \times 3} - \frac{5a \times 2}{12 \times 2} &= \frac{15a - 10a}{24} \\ &= \frac{5a}{24} \quad \blacktriangleleft \end{aligned}$$

LW: Hou die noemer! Moenie daarmee vermenigvuldig nie.

$$\begin{aligned} 5.7 \quad \frac{a^2b^2}{ac^2} \times \frac{4a^2bc}{20b^3} &= \frac{ab^2}{c^2} \times \frac{a^2c}{5b^2} \\ &= \frac{a^3}{5c} \end{aligned}$$

Wanneer ons breuke vermenigvuldig, mag ons FAKTORE kanselleer.

LW: Verstaan die uitdrukking

$$\frac{a \times a \times b \times b}{a \times c \times c} \times \frac{4 \times a \times a \times b \times c}{20 \times b \times b \times b}$$

... en kanselleer daarna!

$$\begin{aligned} 5.8 \quad \frac{6x^5}{x^4} - \frac{15x^3}{3x^2} &= 6x - 5x \\ &= x \quad \blacktriangleleft \end{aligned}$$

... GELYKSOORTIGE TERME ☺

LW: Verstaan die uitdrukking

$$\frac{6 \times x \times \cancel{x} \times \cancel{x} \times \cancel{x} \times \cancel{x}}{\cancel{x} \times \cancel{x} \times \cancel{x} \times \cancel{x}} - \frac{5 \times \cancel{15} \times x \times \cancel{x} \times \cancel{x}}{3 \times \cancel{x} \times \cancel{x}}$$

$$\begin{aligned} 5.9 \quad \frac{2x+1}{4} - \frac{x+2}{2} - \frac{1}{4} &= \frac{2x+1 - 2(x+2) - 1}{4} \\ &= \frac{2x+1 - 2x - 4 - 1}{4} \\ &= \frac{-4}{4} \\ &= -1 \quad \blacktriangleleft \end{aligned}$$

Dit is 'n uitdrukking:

hou die waarde dieselfde; moet dit **nie** vermenigvuldig **nie**!
Alle terme moet oor 'n gemene (dieselfde) noemer geskryf word.

$$\begin{aligned} 5.10 \quad \frac{x-y}{y+x} \times \frac{(x+y)^2}{x-y} &= \frac{\cancel{(x-y)}}{\cancel{(x+y)}} \times \frac{(x+y)^{\cancel{2}}}{\cancel{(x-y)}} \\ &= \frac{x+y}{1} \\ &= x+y \quad \blacktriangleleft \end{aligned}$$

Vergelyk met: $\frac{a}{b} \times \frac{b^2}{a} = b \quad \blacktriangleleft$

$$\begin{aligned} 5.11 \quad \frac{x-2}{2x} - \frac{x-3}{3x} &= \frac{3(x-2) - 2(x-3)}{6x} \\ &= \frac{3x - 6 - 2x + 6}{6x} \\ &= \frac{x}{6x} \\ &= \frac{1}{6} \quad \blacktriangleleft \end{aligned}$$

... Moenie vermenigvuldig nie!
... LW: Hakies!
... Hou die noemer, 6x!



LW:

Dit is slegs wanneer ons **IN VERGELYKINGS** met breuke werk (Bladsy V6, Vraag 4), dat dit **logies** is om albei kante van die vergelyking te vermenigvuldig!

$$\begin{aligned} 5.12 \quad \frac{4x^2}{2a^2} \div \frac{4x}{2a^2} &= \frac{4x^2}{2a^2} \times \frac{2a^2}{4x} \\ &= x \quad \blacktriangleleft \end{aligned}$$

$$\begin{aligned} 5.13 \quad \frac{15x^2y^3 + 9x^2y^3}{8x^2y^3} &= \frac{24x^2y^3}{8x^2y^3} \\ &= 3 \quad \blacktriangleleft \end{aligned}$$

... GELYKSOORTIGE TERME ☺

$$\begin{aligned} 5.14 \quad \frac{5a^2b}{3ab} \div \frac{20a^3b}{27} &= \frac{5a}{3} \times \frac{27}{20a^3b} \\ &= \frac{9}{4a^2b} \quad \blacktriangleleft \end{aligned}$$



$$\begin{aligned}
 5.15 \quad & \frac{5}{b} - \frac{4}{a} - \frac{a-b}{ab} \quad \dots \text{Moenie vermenigvuldig nie!} \\
 &= \frac{5a - 4b - (a - b)}{ab} \quad \dots \text{LW: Hakies!} \\
 &= \frac{5a - 4b - a + b}{ab} \quad \dots \text{Hou die noemer, ab!} \\
 &= \frac{4a - 3b}{ab} \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 5.16 \quad & \frac{3a^{-2}b \times 24b^{-1}a^{-1}}{9a^{-4}b^{-3}} \\
 &= \frac{72a^{-3}}{9a^{-4}b^{-3}} \\
 &= 8ab^3 \blacktriangleleft \quad \dots \frac{a^{-3}}{a^{-4}} = a^{-3-(-4)} = a^1 \\
 &\quad \& \frac{1}{b^{-3}} = b^3
 \end{aligned}$$

$$\begin{aligned}
 5.17 \quad & \frac{x^2}{2} + \frac{2x^2}{3} - \frac{7x^2}{6} \\
 &= \frac{3x^2 + 2(2x^2) - 7x^2}{6} \quad \dots \text{Skryf al 3 terme oor 'n gemene noemer, 6.} \\
 &= \frac{3x^2 + 4x^2 - 7x^2}{6} \quad \dots \text{Moenie vermenigvuldig (met 6) nie!} \\
 &= \frac{0}{6} \\
 &= 0 \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 5.18 \quad & \frac{6x^2}{7xy} \times \frac{3y^3}{2x} \\
 &= \frac{6x}{7y} \times \frac{3y^3}{2x} \\
 &= \frac{9y^2}{7} \blacktriangleleft
 \end{aligned}$$



Vierkantswortels en derdemagswortels

$$\begin{aligned}
 5.19 \quad & \sqrt{225x^4} - \sqrt[3]{125x^6} \\
 &= 15x^2 - 5x^2 \\
 &= 10x^2 \blacktriangleleft
 \end{aligned}$$

$$\begin{array}{r}
 3 \overline{)225} \\
 3 \overline{)75} \\
 5 \overline{)25} \\
 \hline
 5
 \end{array}$$

$$\therefore 225 = 3^2 \times 5^2$$

$$\therefore \sqrt{225} = 3 \times 5$$

$$\begin{array}{r}
 5 \overline{)125} \\
 5 \overline{)25} \\
 \hline
 5
 \end{array}$$

$$\therefore 125 = 5^3$$

$$\therefore \sqrt[3]{125} = 5$$

$$\begin{aligned}
 5.20 \quad & \sqrt{16x^{16} \times 25x^4} \quad \left[\text{OF: } = \sqrt{400x^{20}} \right] \\
 &= \sqrt{16x^{16}} \cdot \sqrt{25x^4} \\
 &= 4x^8 \cdot 5x^2 \\
 &= 20x^{10} \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 5.21 \quad & \sqrt[3]{27x^{27}} \quad \dots \left[\begin{array}{l} 3 \times 3 \times 3 = 27; \\ x^9 \times x^9 \times x^9 = x^{27} \end{array} \right] \\
 &= 3x^9 \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 5.22 \quad & \sqrt{16a^2 + 9a^2} \quad \dots \text{tel eers GELYKSOORTIGE TERME op} \\
 &= \sqrt{25a^2} \\
 &= 5a \blacktriangleleft
 \end{aligned}$$

LW: $\sqrt{16a^2 + 9a^2} \neq 4a + 3a!$

$$\begin{aligned}
 6.1 \quad & 4ab(5a^2b^2 + 2ab - 3) \\
 &= 20a^3b^3 + 8a^2b^2 - 12ab \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 6.2 \quad & 3a^2bc^2(3a^2 - 4b - c) \\
 &= 9a^4bc^2 - 12a^2b^2c^2 - 3a^2bc^3 \blacktriangleleft
 \end{aligned}$$

Distributiewe Eienskap:

$$a(b + c) = ab + ac$$

en

$$a(b - c) = ab - ac$$



$$\begin{aligned}
 6.3 \quad & (x + 5)(x + 2) = x^2 + 2x + 5x + 10 \\
 &= x^2 + 7x + 10
 \end{aligned}$$

$$\begin{aligned}
 6.4 \quad & (x - 2)(x - 3) = x^2 - 3x - 2x + 6 \\
 &= x^2 - 5x + 6
 \end{aligned}$$

$$\begin{aligned}
 6.5 \quad & (x + 7)(x - 1) = x^2 - x + 7x - 7 \\
 &= x^2 + 6x - 7
 \end{aligned}$$

$$\begin{aligned}
 6.6 \quad & (2x - 3)(x + 1) \\
 &= 2x^2 + 2x - 3x - 3 \\
 &= 2x^2 - x - 3 \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 6.7 \quad & x(x + 2) - (x - 1)(x - 3) \\
 &= x^2 + 2x - (x^2 - 3x - x + 3) \\
 &= x^2 + 2x - (x^2 - 4x + 3) \\
 &= x^2 + 2x - x^2 + 4x - 3 \\
 &= 6x - 3 \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 6.8 \quad & (x - 3)^2 - x(x + 4) \\
 &= x^2 - 6x + 9 - x^2 - 4x \\
 &= -10x + 9 \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 & (x - 3)^2 \\
 &= (x - 3)(x - 3) \\
 &= x^2 - 3x - 3x + 9 \\
 &= x^2 - 6x + 9
 \end{aligned}$$

Volkome Vierkant Drieterm

$$\begin{aligned}
 6.9 \quad & (2x-1)^2 - (x+1)(x-1) \\
 &= (2x-1)(2x-1) - (x^2-1) \\
 &= 4x^2 - 4x + 1 - x^2 + 1 \\
 &= 3x^2 - 4x + 2 \quad \blacktriangleleft
 \end{aligned}$$

Volkome Vierkant Drieterm

Verskil van Vierkante

$$\begin{aligned}
 (2x-1)^2 &= (2x-1)(2x-1) \\
 &= 4x^2 - 2x - 2x + 1 \\
 &= 4x^2 - 4x + 1
 \end{aligned}$$

$$\begin{aligned}
 \& \quad (x+1)(x-1) &= x^2 - x + x - 1 \\
 &= x^2 - 1
 \end{aligned}$$

$$\begin{aligned}
 6.10 \quad & 2(x+2)^2 - (2x-1)(x+2) \\
 &= 2(x+2)(x+2) - (2x^2 + 4x - x - 2) \\
 &= 2(x^2 + 4x + 4) - (2x^2 + 3x - 2) \\
 &= 2x^2 + 8x + 8 - 2x^2 - 3x + 2 \\
 &= 5x + 10 \quad \blacktriangleleft
 \end{aligned}$$

Volkome Vierkant Drieterm

$$\begin{aligned}
 (x+2)^2 &= (x+2)(x+2) \\
 &= x^2 + 2x + 2x + 4 \\
 &= x^2 + 4x + 4
 \end{aligned}$$



**7.1 → 7.4:
Volkome Vierkant Drieterme**

$$\begin{aligned}
 7.1 \quad & (x+5)^2 = (x+5)(x+5) \\
 &= x^2 + 5x + 5x + 25 \\
 &= x^2 + 10x + 25 \quad \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 7.2 \quad & (p-3)^2 = (p-3)(p-3) \\
 &= p^2 - 3p - 3p + 9 \\
 &= p^2 - 6p + 9 \quad \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 7.3 \quad & (2a+3)^2 = (2a+3)(2a+3) \\
 &= 4a^2 + 6a + 6a + 9 \\
 &= 4a^2 + 12a + 9 \quad \blacktriangleleft
 \end{aligned}$$

$$\begin{aligned}
 7.4 \quad & (4x-1)^2 = (4x-1)(4x-1) \\
 &= 16x^2 - 4x - 4x + 1 \\
 &= 16x^2 - 8x + 1 \quad \blacktriangleleft
 \end{aligned}$$



**7.5 → 7.8:
Verskil van Vierkante**

$$7.5 \quad (x+5)(x-5) = x^2 - 5x + 5x - 25 = x^2 - 25$$

$$7.6 \quad (p-3)(p+3) = p^2 + 3p - 3p - 9 = p^2 - 9$$

$$7.7 \quad (2a+3)(2a-3) = 4a^2 - 6a + 6a - 9 = 4a^2 - 9$$

$$7.8 \quad (4x-1)(4x+1) = 16x^2 + 4x - 4x - 1 = 16x^2 - 1$$



**7.9 → 7.12:
Let op hoe die drieterm
in elke geval verkry word.**

$$7.9 \quad (x+3)(x+4) = x^2 + 4x + 3x + 12 = x^2 + 7x + 12 \quad \blacktriangleleft$$

$$7.10 \quad (x-3)(x-4) = x^2 - 4x - 3x + 12 = x^2 - 7x + 12 \quad \blacktriangleleft$$

$$7.11 \quad (x+3)(x-4) = x^2 - 4x + 3x - 12 = x^2 - x - 12 \quad \blacktriangleleft$$

$$7.12 \quad (x-3)(x+4) = x^2 + 4x - 3x - 12 = x^2 + x - 12 \quad \blacktriangleleft$$

$$\begin{aligned}
 8.1 \quad & \mathbf{B} \quad \blacktriangleleft \quad \dots -(-2)^2 - (2(-2) - 1) \\
 &= -(4) - (-4 - 1) \\
 &= -4 - (-5) \\
 &= -4 + 5 \\
 &= 1
 \end{aligned}$$

$$8.2 \quad \mathbf{C} \quad \blacktriangleleft$$

$$8.3 \quad \mathbf{D} \quad \blacktriangleleft \quad \dots \frac{x}{y} - \frac{1 \times y}{1 \times y} = \frac{x-y}{y} \quad \dots \text{Skryf die terme oor dieselfde noemer.}$$

$$\begin{aligned}
 8.4 \quad & \mathbf{D} \quad \blacktriangleleft \quad \dots \left(\frac{x}{3} - 3y\right)\left(\frac{x}{3} + 3y\right) \\
 &= \left(\frac{x}{3}\right)^2 - (3y)^2 \quad \dots \text{verskil van vierkante} \\
 &= \frac{x^2}{9} - 9y^2
 \end{aligned}$$

FAKTORISERING

1. Gemene Faktor

Toets elke antwoord deur terug te vermenigvuldig (na die begin)



$$1.1 \quad 8p^3 + 4p^2 = 4p^2(2p + 1) \quad \leftarrow$$

$$1.2 \quad 10t^2 - 5t = 5t(2t - 1) \quad \leftarrow$$

$$1.3 \quad 3x^2y - 9xy^2 + 12x^3y^3 = 3xy(x - 3y + 4x^2y^2) \quad \leftarrow$$

$$1.4 \quad 2p^2 + 2 = 2(p^2 + 1) \quad \leftarrow$$

$$1.5 \quad 2(x + y) + a(x + y) = (x + y)(2 + a) \quad \leftarrow$$

$$1.6 \quad 2(x + y) - t(x + y) = (x + y)(2 - t) \quad \leftarrow$$

$$1.7 \quad tx - ty - 2x + 2y = (tx - ty) - (2x - 2y) = t(x - y) - 2(x - y) = (x - y)(t - 2) \quad \leftarrow$$



2. Verskil van vierkante

Toets elke antwoord deur terug te vermenigvuldig (na die begin)



$$2.1 \quad 4x^2 - y^2 = (2x + y)(2x - y) \quad \leftarrow$$

$$2.2 \quad 4x^2 - 4y^2 = 4(x^2 - y^2) = 4(x + y)(x - y) \quad \leftarrow$$

Vergelyk Vraag 2.1 en Vraag 2.2!

In Vraag 2.1: 4 is **nie** 'n gemene faktor nie.
In Vraag 2.2: 4 is 'n gemene faktor.



$$2.3 \quad 81 - 100a^2 = (9 + 10a)(9 - 10a) \quad \leftarrow$$

$$2.4 \quad 9p^2 - 36q^2 = 9(p^2 - 4q^2) = 9(p + 2q)(p - 2q) \quad \leftarrow$$

$$2.5 \quad 7x^2 - 28 = 7(x^2 - 4) = 7(x + 2)(x - 2) \quad \leftarrow$$



3. Drieterme

3 TERME

Let op hierdie **PRODUKTE**:

► **Volkome Vierkante** → **Volkome Vierkant DRIETERME**

$$\begin{aligned} (x+3)^2 &= (x+3)(x+3) = x^2 + 3x + 3x + 9 = x^2 + 6x + 9 \\ \& \ (x-3)^2 &= (x-3)(x-3) = x^2 - 3x - 3x + 9 = x^2 - 6x + 9 \\ \therefore x^2 + 6x + 9 &= (x + 3)^2 \\ \& \ x^2 - 6x + 9 &= (x - 3)^2 \end{aligned}$$

$$\begin{aligned} (a+b)^2 &= (a+b)(a+b) = a^2 + ab + ab + b^2 = a^2 + 2ab + b^2 \\ \& \ (a-b)^2 &= (a-b)(a-b) = a^2 - ab - ab + b^2 = a^2 - 2ab + b^2 \\ \therefore a^2 + 2ab + b^2 &= (a + b)^2 \\ \& \ a^2 - 2ab + b^2 &= (a - b)^2 \end{aligned}$$



► **Ander produkte** → **DRIETERME**

$$\begin{aligned} (x+2)(x+3) &= x^2 + 2x + 3x + 6 = x^2 + 5x + 6 \\ (x-2)(x-3) &= x^2 - 2x - 3x + 6 = x^2 - 5x + 6 \\ (x+2)(x-3) &= x^2 + 2x - 3x - 6 = x^2 - x - 6 \\ (x-2)(x+3) &= x^2 - 2x + 3x - 6 = x^2 + x - 6 \end{aligned}$$

Kyk na die resultate hierbo om faktorisering van drieterme te verstaan



Toets elke antwoord deur terug te vermenigvuldig (na die begin)



$$3.1 \quad a^2 + 8a + 16 = (a + 4)(a + 4) = (a + 4)^2 \quad \leftarrow$$

$$3.2 \quad p^2 - 10p + 25 = (p - 5)(p - 5) = (p - 5)^2 \quad \leftarrow$$

$$3.3 \quad x^2 + 5x + 6 = (x + 3)(x + 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & +3 \\ \times & +2 \\ \hline 1 & +2 \\ & +5 \end{array}$$

$$3.4 \quad x^2 - 5x + 6 = (x - 3)(x - 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & -3 \\ \times & -2 \\ \hline 1 & -2 \\ & -5 \end{array}$$

$$3.5 \quad x^2 + x - 6 = (x + 3)(x - 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & +3 \\ \times & -2 \\ \hline 1 & -2 \\ & +1 \end{array}$$

$$3.6 \quad x^2 - x - 6 = (x - 3)(x + 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & -3 \\ \times & +2 \\ \hline 1 & +2 \\ & -1 \end{array}$$

$$3.7 \quad x^2 - 11x + 18 = (x - 9)(x - 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & -9 \\ \times & -2 \\ \hline 1 & -2 \\ & -11 \end{array}$$

$$3.8 \quad x^2 + 11x + 18 = (x + 9)(x + 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & +9 \\ \times & +2 \\ \hline 1 & +2 \\ & +11 \end{array}$$

$$3.9 \quad x^2 - 7x - 18 = (x - 9)(x + 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & -9 \\ \times & +2 \\ \hline 1 & +2 \\ & -7 \end{array}$$

$$3.10 \quad x^2 + 7x - 18 = (x + 9)(x - 2) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & \times 9 \\ 1 & -2 \\ \hline & +7 \end{array}$$

$$3.11 \quad x^2 + 9x + 18 = (x + 6)(x + 3) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & \times 6 \\ 1 & +3 \\ \hline & +9 \end{array}$$

$$3.12 \quad x^2 - 9x + 18 = (x - 6)(x - 3) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & \times 6 \\ 1 & -3 \\ \hline & -9 \end{array}$$

$$3.13 \quad x^2 + 3x - 18 = (x + 6)(x - 3) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & \times 6 \\ 1 & -3 \\ \hline & +3 \end{array}$$

$$3.14 \quad x^2 - 3x - 18 = (x - 6)(x + 3) \quad \leftarrow \quad \dots \quad \begin{array}{r|l} 1 & \times 6 \\ 1 & +3 \\ \hline & -3 \end{array}$$

FAKTORISERING

Daar is **3 Tipes** faktorisering:

- ❶ **Gemene Faktor (GF):** Probeer altyd hierdie eerste!
- ❷ **Verskil van Vierkante (VvV):** 2 terme
- ❸ **Drieterme:** 3 terme

HERKEN HIERDIE!



Gemengde Faktorisering

Toets elke antwoord deur terug te vermenigvuldig (na die begin)



$$4.1 \quad 3a^3 - 9a^2 - 6a = 3a(a^2 - 3a - 2) \quad \leftarrow \quad \dots \text{ let wel: hierdie faktoreer nie verder nie}$$

$$4.2 \quad 2a^2 - 18a + 36 = 2(a^2 - 9a + 18) = 2(a - 6)(a - 3) \quad \leftarrow \quad \begin{array}{r|l} 1 & \times 6 \\ 1 & -3 \\ \hline & -9 \end{array}$$

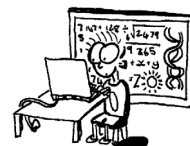
$$4.3 \quad 4(a + b) - x^2(a + b) = (a + b)(4 - x^2) = (a + b)(2 + x)(2 - x) \quad \leftarrow \quad \dots \text{ toets altyd of jy verder kan faktoreer}$$

$$4.4 \quad 6x^3(a - b) + x(b - a) = 6x^3(a - b) - x(a - b) = (a - b)(6x^3 - x) = (a - b) \cdot x(6x^2 - 1) = x(a - b)(6x^2 - 1) \quad \leftarrow \quad \dots \text{ omruiling}$$

$$4.5 \quad 6a^3 - 12a^2 + 18a = 6a(a^2 - 2a + 3) \quad \leftarrow \quad \dots \text{ let wel: hierdie faktoreer nie verder nie}$$

Gebruik faktorisering om die volgende breuke te vereenvoudig

$$5.1 \quad \frac{x^2 - 1}{3x + 3} \quad \dots \text{ VvV} \quad \dots \text{ GF} \\ = \frac{(x - 1)(x + 1)}{3(x + 1)} \\ = \frac{x - 1}{3} \quad \leftarrow$$



$$5.2 \quad \frac{x^2 - 4x}{x^2 - 2x - 8} \quad \dots \text{ GF} \quad \dots \text{ Drieterm} \quad \dots \quad \begin{array}{r|l} 1 & \times 4 \\ 1 & +2 \\ \hline & -2 \end{array} \\ = \frac{x(x - 4)}{(x - 4)(x + 2)} \\ = \frac{x}{x + 2} \quad \leftarrow$$



$$5.3 \quad \frac{3a - 6b}{4b - 2a} \quad \dots \text{ Gemene Faktore} \\ = \frac{3(a - 2b)}{2(2b - a)} \\ = \frac{3(a - 2b)}{-2(a - 2b)} \quad \dots \quad 2b - a = -(a - 2b) \\ = -\frac{3}{2} \quad \leftarrow$$

$$5.4 \quad \frac{2x^2 - 8}{3x - 12} \times \frac{x^2 - 4x}{x - 2} \\ = \frac{2(x^2 - 4)}{3(x - 4)} \times \frac{x(x - 4)}{x - 2} \\ = \frac{2(x + 2)(x - 2)}{3(x - 2)} \\ = \frac{2(x + 2)}{3} \quad \leftarrow$$



Moenie afgeskrik word deur hoe hierdie breuke lyk nie!

Fokus net op faktorisering waar moontlik; kanselleer daarna die faktore waar moontlik.

$$5.5 \quad \frac{x^2 + 2x}{x^3 - 2x} \div \frac{x^2 - 4}{x - 2} \\ = \frac{x^2 + 2x}{x^3 - 2x} \times \frac{x - 2}{x^2 - 4} \quad \dots \text{ let op die 'omgekeerde' breuk!} \\ = \frac{x(x + 2)}{x(x^2 - 2)} \times \frac{(x - 2)}{(x + 2)(x - 2)} \\ = \frac{1}{x^2 - 2} \quad \leftarrow$$

ALGEBRAÏESE VERGELYKINGS (Lineêr en Kwadratiese)

LOGIKA IS DIE SLEUTEL!



- 1.1 **B** ◀ ... As 3 'n wortel is, dan sal $x = 3$
die vergelyking waar maak

$$\begin{aligned} \text{d.w.s. } 3^2 + 3 + t &= 0 \\ \therefore 9 + 3 + t &= 0 \\ \therefore t &= -12 \end{aligned}$$

- 1.2 **D** ◀ ... $2p + 12 = 58$
 $\therefore 2p = 46$
 $\therefore p = 23$

$$\begin{aligned} \text{[OF: } ? + 12 &= 58 \\ \text{Antwoord: } 46 \\ \text{Dus, } 2p &= 46 \\ \therefore 2 \times ? &= 46 \\ \therefore p &= 23 \end{aligned}$$

- 1.3 **B** ◀ ... **As** $(x-1)(x+2) = 0$,
dan is $x-1 = 0$ **of** $x+2 = 0$
 $\therefore x = 1$ $\therefore x = -2$

- 1.4 **D** ◀ ... $\frac{3x}{2} = -6$
 $\therefore 3x = -12$
 $x = -4$

$$\begin{aligned} \text{[OF: } \frac{?}{2} &= -6 \\ \text{Antwoord: } -12 \\ \therefore 3x &= -12 \\ \text{Dus, } 3 \times ? &= -12 \\ \therefore x &= -4 \end{aligned}$$

- 1.5 **B** ◀ ... Die produk van 'n getal, x , en 6 is gelyk aan
 $x \times 6 = 6x$

- 2.1 $x + 5 = 2$... '5 meer as 'n getal is 2'
 $\therefore x = -3$ ◀
- 2.2 $x - 3 = -4$... '3 minder as 'n getal is -4'
 $\therefore x = -1$ ◀
- 2.3 $2x = 12$... 'dubbel 'n getal is 12'
 $\therefore x = 6$ ◀
- 2.4 $\frac{x}{5} = 6$... 'n vyfde van 'n getal is 6'
 $\therefore x = 30$ ◀

Toets jou antwoord deur substitusie in die gegewe vergelyking om te sien of dit 'waar' is vir die waarde van x .

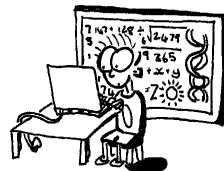


- 3.1 $3x - 1 = 5$
 $\therefore 3x = 6$
 $\therefore x = 2$ ◀

[Toets: LK = $3x - 1 = 3(2) - 1 = 5 = \text{RK} \checkmark$]

- 3.2 $2(x + 1) = 10$
 $\therefore 2x + 2 = 10$... $\text{[OF: } x + 1 = 5$
 $\therefore 2x = 8$ $\therefore x = 4$ ◀

[Toets: LK = $2(4 + 1) = 2 \times 5 = 10 = \text{RK} \checkmark$]



- 3.3 $8x + 3 = 3x - 22$
 $\therefore 8x - 3x = -22 - 3$... Trek 3x af & Trek 3 af
 $\therefore 5x = -25$
 $\therefore x = -5$ ◀ ... $\text{[} \div 5, \text{ OF: } 5 \times ? = -25 \text{]}$

Toets: **LK** = $8(-5) + 3 = -40 + 3 = -37$
& **RK** = $3(-5) - 22 = -15 - 22 = -37$
 $\therefore \text{LK} = \text{RK} \checkmark$ $\therefore$ Die antwoord is korrek.
d.w.s. Die vergelyking is 'waar' vir $x = -5$.
Ons sê dat -5 die **wortel** (of oplossing) van die vergelyking is.

- 3.4 $3(x + 6) = 12$
 $\therefore 3x + 18 = 12$... $\text{[OF: } x + 6 = 4$
 $\therefore 3x = -6$ $\therefore x = -2$ ◀

Toets jou antwoord deur substitusie in die gegewe vergelyking om te sien of dit 'waar' is vir die waarde van x .

- 3.5 $2x - 5 = 5x + 16$... Tel 5 by & Trek 5x af
 $\therefore 2x - 5x = 16 + 5$
 $\therefore -3x = 21$
 $\therefore x = -7$ ◀ ... Deel deur -3

Toets jou antwoord deur substitusie in die gegewe vergelyking om te sien of dit 'waar' is vir die waarde van x .

- 3.6 $x^3 + x^3 = 2$
 $\therefore 2x^3 = 2$... GELYKSOORTIGE TERME
 $\therefore x^3 = 1$... deel deur 2
 $\therefore x = 1$ ◀ ... neem derdemagswortel

Toets jou antwoord deur substitusie in die gegewe vergelyking om te sien of dit 'waar' is vir die waarde van x .

Vergelykings insluitend breuke

LET WEL: In **UITDRUKKINGS**, die vorige afdeling, het ons **nie** vermenigvuldig **nie**. Ons het die noemer gehou!

Nou, in **VERGELYKINGS** pas ons logika toe en vermenigvuldig !!! – 'wat ons aan die linkerkant (**LK**) van die vergelyking doen, doen ons ook aan die regterkant (**RK**)'.

4.1
$$\frac{x-2}{4} + \frac{2x+1}{3} = \frac{5}{3}$$

x12
$$\therefore 3(x-2) + 4(2x+1) = 4(5)$$

$$\therefore 3x - 6 + 8x + 4 = 20$$

$$\therefore 11x - 2 = 20$$

$$\therefore 11x = 22$$

$$\therefore x = 2 \leftarrow$$

Toets jou antwoord! 

Die KGV van die noemers is 12.
Die logika: $12 \times$ die **LK** = $12 \times$ die **RK**

4.2
$$\frac{x+2}{3} - \frac{x-3}{4} = 0$$

x12
$$\therefore 4(x+2) - 3(x-3) = 0$$

$$\therefore 4x + 8 - 3x + 9 = 0$$

$$\therefore x + 17 = 0$$

$$\therefore x = -17 \leftarrow$$

Toets jou antwoord! 

4.3
$$\frac{2x-3}{2} - \frac{x+1}{3} = \frac{3x-1}{2}$$

x6
$$3(2x-3) - 2(x+1) = 3(3x-1)$$

$$\therefore 6x - 9 - 2x - 2 = 9x - 3$$

$$\therefore 4x - 11 = 9x - 3$$

$$\therefore 4x - 9x = -3 + 11$$

$$\therefore -5x = 8$$

$$\therefore x = -\frac{8}{5} \leftarrow$$

LW:
Hakies!

6 keer die **LK**
= 6 keer die **RK**

Toets jou antwoord!



4.4
$$\frac{x}{1} - \frac{x-1}{2} = \frac{3}{1}$$

x2
$$\therefore 2x - (x-1) = 2(3)$$

$$\therefore 2x - x + 1 = 6$$

$$\therefore x + 1 = 6$$

$$\therefore x = 5 \leftarrow$$

LW: Hakies!

2 keer die **LK**
= 2 keer die **RK**

Toets jou antwoord!



4.5
$$\frac{x+1}{3} - \frac{x-1}{6} = \frac{1}{1}$$

x6
$$\therefore 2(x+1) - (x-1) = 6(1)$$

$$\therefore 2x + 2 - x + 1 = 6$$

$$\therefore x + 3 = 6$$

$$\therefore x = 3 \leftarrow$$

LW: Hakies!

6 keer die **LK**
= 6 keer die **RK**

Toets jou antwoord!



Vergelyk die posisie van die = tekens

In Algebraïese Uitdrukings (in die vorige afdeling):

Die = **tekens** is **links** af

In Algebraïese Vergelykings (V4.1 tot 4.5 hierbo):

Die = **tekens** is in die **middel**
en die **∴ tekens** is aan die **linkerkant**

Kwadratiese Vergelykings

Die LOGIKA:

As die produk van 2 getalle = 0 is, dan moet óf die een óf die ander getal = 0 wees.

5.1 $(x-3)(x+4) = 0$... die produk van $x-3$ en $x+4$ is gelyk aan 0, dus:

Óf $x-3 = 0$ **of** $x+4 = 0$

$\therefore x = 3 \leftarrow$ $\therefore x = -4 \leftarrow$

Toets: As $x = 3$:

LK = $(3-3)(3+4) = 0(7) = 0 = \mathbf{RK} \checkmark$

As $x = -4$:

LK = $(-4-3)(-4+4) = (-7) \times 0 = 0 = \mathbf{RK} \checkmark$

$\therefore$ Albei antwoorde is korrek

5.2 $x^2 - 5x - 6 = 0$... Faktoreer die **drieterm** sodat jy 'n produk het

$\therefore (x-6)(x+1) = 0$

$\therefore$ **Óf** $x-6 = 0$ **of** $x+1 = 0$

$\therefore x = 6 \leftarrow$ $x = -1 \leftarrow$

Toets jou antwoorde!



5.3 $x^2 - 1 = 0$... Faktoreer! **(Verskil van vierkante)**

$\therefore (x+1)(x-1) = 0$

$\therefore$ **Óf** $x+1 = 0$ **of** $x-1 = 0$

$\therefore x = -1 \leftarrow$ $x = 1 \leftarrow$

Toets jou antwoorde!



5.4 $x^2 - 2x = 0$... Faktoreiseer! (**Gemene Faktor**)
 $\therefore x(x-2) = 0$

$\therefore$ **Óf** $x = 0$ **of** $x - 2 = 0$
 $\therefore x = 2$ $\blacktriangleleft$

Toets jou antwoorde!



In Vrae 6.1 en 6.2:

$$\begin{aligned}(x-2)^2 &= (x-2)(x-2) \\ &= x^2 - 2x - 2x + 4 \\ &= x^2 - 4x + 4\end{aligned}$$



In Vraag 6.3:

$$\begin{aligned}(x+3)^2 &= (x+3)(x+3) \\ &= x^2 + 3x + 3x + 9 \\ &= x^2 + 6x + 9\end{aligned}$$

Nou, die vergelykings ...

6.1 $2(x-2)^2 = (2x-1)(x-3)$
 $\therefore 2(x-2)(x-2) = 2x^2 - 6x - x + 3$

$\therefore 2(x^2 - 4x + 4) = 2x^2 - 7x + 3$

$\therefore 2x^2 - 8x + 8 = 2x^2 - 7x + 3$

$\therefore -8x + 7x = 3 - 8$

$\therefore -x = -5$

$\therefore x = 5$ $\blacktriangleleft$

Toets jou antwoorde!



die twee $2x^2$ terme
kanselleer mekaar en
die vergelyking word
lineêr (nie meer
kwadraties) nie.

6.2 $(x-2)^2 + 3x - 2 = (x+3)^2$
 $\therefore (x-2)(x-2) + 3x - 2 = (x+3)(x+3)$

$\therefore x^2 - 4x + 4 + 3x - 2 = x^2 + 6x + 9$

$\therefore -x + 2 = 6x + 9$...

$\therefore -x - 6x = 9 - 2$

$\therefore -7x = 7$

$\therefore x = -1$ $\blacktriangleleft$

Toets jou antwoord!



die twee $2x^2$ terme
kanselleer mekaar
en die vergelyking
word **lineêr**.

6.3 $(x-3)^2 = 16$

$(x-3)(x-3) = 16$

$\therefore x^2 - 6x + 9 - 16 = 0$

$\therefore x^2 - 6x - 7 = 0$ $\blacktriangleleft$ Onthou die logika? Die produk moet = 0 wees!

$\therefore (x-7)(x+1) = 0$ $\blacktriangleleft$ Die **drieterm** is gefaktoreiseer

Die logika:

$(x-7)$ keer $(x+1)$ is gelyk aan 0, dus is

Óf $x - 7$ gelyk aan 0 **of** $x + 1$ gelyk aan 0

d.w.s. **Óf** $x - 7 = 0$ **of** $x + 1 = 0$

$\therefore x = 7$ $\blacktriangleleft$ **of** $x = -1$ $\blacktriangleleft$

Toets jou antwoorde!



Ander ...

Let Wel:

Die oplossing van vergelykings vereis
die **omkeer van bewerking**s



$+$ $\leftrightarrow$ $-$

$\times$ $\leftrightarrow$ $\div$

magte $\leftrightarrow$ wortels

$x + 3 = 8$

$\therefore x + 3 - 3 = 8 - 3$

$\therefore x = 5$ $\blacktriangleleft$

$3x = 12$

$\therefore \frac{3x}{3} = \frac{12}{3}$

$\therefore x = 4$ $\blacktriangleleft$

$x^3 = 8$

Neem $\sqrt[3]{}$ aan albei kante

$\therefore x = 2$ $\blacktriangleleft$

Let Wel: $x^2 = 9$
 $\therefore x = \pm 3$

As die mag ewe is,
dan is daar 2 wortels!

$x - 3 = 8$

$\therefore x - 3 + 3 = 8 + 3$

$\therefore x = 11$ $\blacktriangleleft$

$\frac{x}{3} = 12$

$\therefore \frac{x}{3} \times 3 = 12 \times 3$

$\therefore x = 36$ $\blacktriangleleft$

$\sqrt{x} = 5$

Kwadreer albei kante

$(\sqrt{x})^2 = 5^2$

$\therefore x = 25$ $\blacktriangleleft$



TOETS ALTYD YOU ANTWOORD!

Dus, los op vir x:

(a) $\sqrt{x} = 2$

Kwadreer albei kante

$\therefore x = 4$ $\blacktriangleleft$

(b) $\sqrt{\sqrt{x}} = 2$

Kwadreer albei kante

$\therefore \sqrt{x} = 4$

Kwadreer albei kante weer

$\therefore x = 16$ $\blacktriangleleft$

Sien nou V7.1

7.1

$$\sqrt{\sqrt{\sqrt{x}}} = 2$$

Kwadreer albei kante

$$\therefore (\sqrt{\sqrt{\sqrt{x}}})^2 = (2)^2$$

$$\therefore \sqrt{\sqrt{x}} = 4$$

Kwadreer albei kante weer

$$\therefore (\sqrt{\sqrt{x}})^2 = (4)^2$$

$$\therefore \sqrt{x} = 16$$

Kwadreer albei kante weer!

$$\therefore (\sqrt{x})^2 = (16)^2$$

$$\therefore x = 256 \quad \blacktriangleleft$$

Toets jou antwoord!



7.2

$$\sqrt{\frac{1}{\sqrt{x}}} = 2$$

$$\therefore \left(\sqrt{\frac{1}{\sqrt{x}}}\right)^2 = (2)^2$$

$$\therefore \frac{1}{\sqrt{x}} = 4$$

$$\therefore \left(\frac{1}{\sqrt{x}}\right)^2 = (4)^2$$

$$\therefore \frac{1}{x} = \frac{16}{1}$$

$$\therefore x = \frac{1}{16} \quad \blacktriangleleft$$

Toets jou antwoord!



NOTAS



GRAFIEKE

1.1 B ◀ ... $f(x) = 2x + 4$:

- positiewe gradiënt van $\frac{2}{1}$... **2x**,
- y-afsnit van 4 ... $y = 4$ wanneer $x = 0$

As 'n punt op 'n lyn lê, dan sal die **vergelyking** van die grafiek **waar** wees vir sy koördinate. (Sien Vraag 1.2)

1.2 D ◀ ... Die vergelyking is $y = x$, dus sal x en y gelyk moet wees (d.w.s. die koördinate moet dieselfde waarde hê)

1.3 B ◀ ... $\frac{d}{6} = \frac{2}{3}$ ∴ $d = 4$... ekwivalente breuke

Baie belangrik om te weet:

Op die **Y-as**, is die **x**-koördinaat (altyd) **0** (Sien Vraag 1.4)

Op die **X-as**, is die **y**-koördinaat (altyd) **0** (Sien Vraag 1.5)

1.4 C ◀ ... Stel $x = 0$ in; dan is

$$y\text{-afsnit: } 4(0) + 2y = 12$$

$$\therefore 2y = 12$$

$$\therefore y = 6$$

[Dus is die punt op die y-as (0; 6)]

1.5 B ◀ ... Stel $y = 0$; dan is

$$x\text{-afsnit: } 3(0) + 2x + 1 = 0$$

$$\therefore 2x = -1$$

$$\therefore x = -\frac{1}{2}$$

∴ $\left(-\frac{1}{2}; 0\right)$... die koördinate van die x-afsnit

2. P is die snypunt van die lyne $y = x$ en $y = 3$ en dus moet albei hierdie vergelykings by punt P 'waar wees'. Dus moet y gelyk wees aan x en y moet gelyk wees aan 3.

$$\therefore y = x = 3$$

$$\therefore \mathbf{P(3; 3)}$$

3.1 $y = 3x - 5$

x	-2	-1	0	1
y	-11	-8	-5	-2

$$y = 3(-2) - 5 = -11$$

$$y = 3(-1) - 5 = -8$$

$$y = 3(0) - 5 = -5$$

$$y = 3(1) - 5 = -2$$

Ons vervang die waardes van x in die vergelyking om y te bepaal.

3.2 $y = -\frac{2}{3}x - 1$

x	-3	-1	0	1
y	1	$-\frac{1}{3}$	-1	$-\frac{5}{3}$

$$y = -\frac{2}{3}\left(-\frac{3}{1}\right) - 1 = 2 - 1 = 1$$

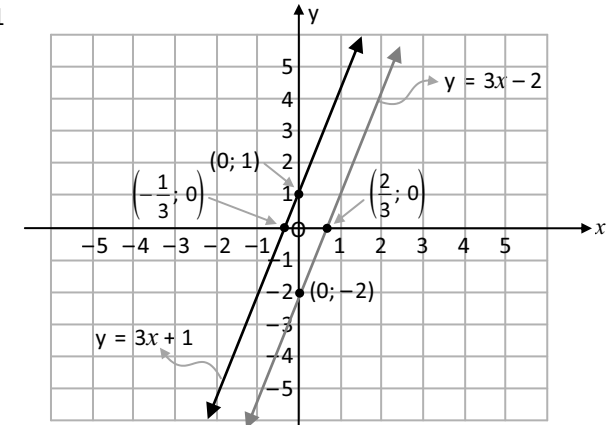
$$y = -\frac{2}{3}(-1) - 1 = \frac{2}{3} - 1 = -\frac{1}{3}$$

$$y = -\frac{2}{3}(0) - 1 = -1$$

$$y = -\frac{2}{3}(1) - 1 = -\frac{2}{3} - 1 = -\frac{5}{3}$$



4.1



Om die punte te bepaal waar die grafieke die asse sny:

$y = 3x - 2$:

Vir die **Y-afsnit**, stel $x = 0$ in

$$\therefore y = 3(0) - 2 = -2$$

∴ Die grafiek sny die **y-as** by -2.

Die **punt** is **(0; 2)**

$y = 3x + 1$:

$$\therefore y = 3(0) + 1 = 1$$

∴ Die grafiek sny die **y-as** by 1.

Die **punt** is **(0; 1)**

Vir die **X-afsnit**, stel $y = 0$ in

$$\therefore 0 = 3x - 2$$

$$\therefore 3x = 2$$

$$\therefore x = \frac{2}{3}$$

∴ Die grafiek sny die **x-as** by $\frac{2}{3}$.

Die **punt** is $\left(\frac{2}{3}; 0\right)$

$$\therefore 0 = 3x + 1$$

$$\therefore 3x = -1$$

$$\therefore x = -\frac{1}{3}$$

∴ Die grafiek sny die **x-as** by $-\frac{1}{3}$.

Die **punt** is $\left(-\frac{1}{3}; 0\right)$

4.2 Hulle is parallel < ... hulle het gelyke gradiënte

5.1 **AD:** Die gradiënt = $-\frac{4}{2} = -2$... $\therefore m = -2$
& die y-afsnit is 4 ... $\therefore c = 4$

$\therefore$ Die vergelyking is $y = -2x + 4$ < ... $m = -2$ & $c = 4$
in $y = mx + c$

BC: Die gradiënt = $-\frac{4}{2} = -2$... $\therefore m = -2$
& die y-afsnit is -4 ... $\therefore c = -4$

$\therefore$ Die vergelyking is $y = -2x - 4$ < ... $m = -2$ & $c = -4$
in $y = mx + c$

Die standaardvorm van die vergelyking van 'n reguitlyn is **$y = mx + c$** , waar
m = die gradiënt en **c** = die y-afsnit.

5.2 Hulle is parallel.
Hulle het albei gradiënte van -2 .



Albei gradiënte is negatief en word gemeet as $\frac{\text{aantal eenhede afwaarts}}{\text{aantal eenhede dwarsoor}}$
d.w.s. $\frac{\text{vertikale verandering}}{\text{horizontale verandering}}$

6.1 Die gradiënt = $-\frac{5}{1} = -5$ <

Deur inspeksie

- negatiewe gradiënt
- $\frac{\text{rise}}{\text{run}}$ of $\frac{\text{vertikale verandering}}{\text{horizontale verandering}}$

Dus, — en **5 eenhede afwaarts**
1 eenheid dwarsoor

Die gebruik van 'n formule vir die gradiënt is nie ideaal vir Graad 9-leerders nie.

6.2 $y = -5x + 5$ < ... gradiënt, $m = -5$ & y-afsnit, $c = 5$

6.3 Die gradiënt van enige ander reguitlyn parallel tot hierdie lyn getrek is -5 . < ... *parallele lyne het dieselfde gradiënt*

7.1

	A	B	C
x-koördinaat	0	2	4
y-koördinaat	-2	0	2



Let Wel: $x = 0$ op die **y-as** (by A)
& $y = 0$ op die **x-as** (by B)

7.2 $y = x - 2$ < ... Deur inspeksie:
Die y-koördinaat is almal 2 minder as die x-koördinaat.

of: Gradiënt = $+\frac{2}{2} = 1$
& y-afsnit, $c = -2$

8.1 Die vergelyking van CD: $x = 2$ <

... want elke punt op (vertikale) lyn CD het 'n x-koördinaat gelyk aan 2

$\therefore x = 2$ is die **vergelyking** van CD



Die vergelyking van 'n lyn is 'n 'reël' wat waar is vir alle punte op die lyn.

8.2 Die vergelyking van AB: $y = 2x$ <

Metode 1:

Kyk na verskeie punte op die grafiek:

bv. $(-2; -4)$; $(-1; -2)$; $(1; 2)$

en let op dat y altyd gelyk is aan twee keer x

Metode 2:

m, die gradiënt = $+\frac{2}{1} = 2$

& c, die y-afsnit, is 0

8.3 **E(2; -2)** < ... $x = 2$ en $y = -2$ by punt E

8.4 **CE = 6 eenhede** < ... $CE = CD + DE = 4 + 2 = 6$ eenhede

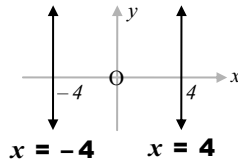
OF $CE = Y_C - Y_E$... die verskil van die y-koördinate van C en E.
 $= 4 - (-2)$
 $= 6$



Antwoorde: Grafieke

- 9.1 Die lyne $x = 4$ en $x = -4$ is **parallel** aan mekaar. ◀

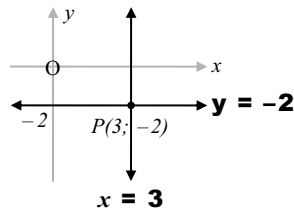
... Die lyne $x = 4$ en $x = -4$:
is albei parallel aan die y -as



- 9.2 Die vergelyking van die horisontale lyn deur die punt $P(3; -2)$ is **$y = -2$** . ◀

... Die horisontale lyn deur
 $P(3; -2)$ is **$y = -2$** ;

Die vertikale lyn deur
 $P(3; -2)$ is **$x = 3$** ;



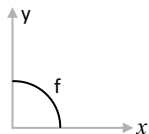
- 9.3 Die gradiënt van die lyn gedefinieer deur $y - 4x + 5 = 0$ is gelyk aan **4**. ◀

... $y - 4x + 5 = 0$

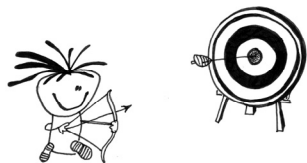
$$\therefore y = 4x - 5 \quad \dots y = mx + c$$

$\therefore$ Die gradiënt, wat die koëffisiënt van x is, is **4**

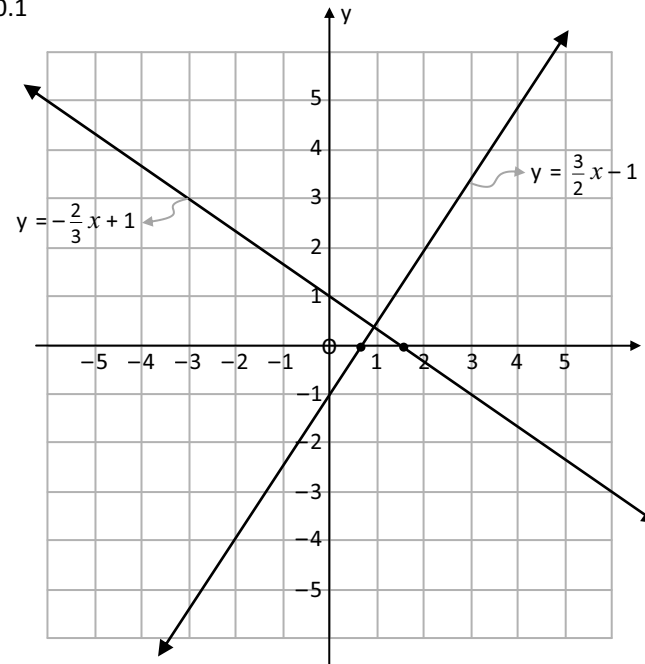
- 9.4 Die grafiek van f hieronder stel 'n **niet-lineêre** funksie voor. ◀



... 'n Lineêre funksie
is 'n reguitlyn,
nie 'n kurwe nie.



10.1



Om die punte te bepaal waar die grafieke die asse sny :

$$y = -\frac{2}{3}x + 1:$$

$$y = \frac{3}{2}x - 1:$$

Vir die **Y-afsnit**, stel $x = 0$ in

$$\begin{aligned} \therefore y &= -\frac{2}{3}(0) + 1 \\ &= 1 \end{aligned}$$

$\therefore$ Die grafiek sny die
y-as by 1.

Die **punt** is **(0; 1)**

$$\begin{aligned} \therefore y &= \frac{3}{2}(0) - 1 \\ &= -1 \end{aligned}$$

$\therefore$ Die grafiek sny die
y-as by -1.

Die **punt** is **(0; -1)**

Vir die **X-afsnit**, stel **$y = 0$** in

$$\therefore 0 = -\frac{2}{3}x + 1$$

$$\therefore \frac{2}{3}x = 1$$

$$\therefore 2x = 3 \quad \dots \times 3$$

$$\therefore x = \frac{3}{2} \quad \dots \div 2$$

$\therefore$ Die grafiek sny die
x-as by $\frac{3}{2}$.

Die **punt** is **$(\frac{3}{2}; 0)$**

$$\therefore 0 = \frac{3}{2}x - 1$$

$$\therefore \frac{3}{2}x = 1$$

$$\therefore 3x = 2 \quad \dots \times 2$$

$$\therefore x = \frac{2}{3} \quad \dots \div 3$$

$\therefore$ Die grafiek sny die
x-as by $\frac{2}{3}$.

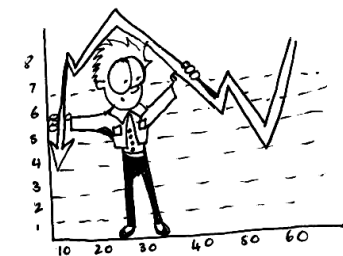
Die **punt** is **$(\frac{2}{3}; 0)$**

- 10.2 Hulle is loodreg.

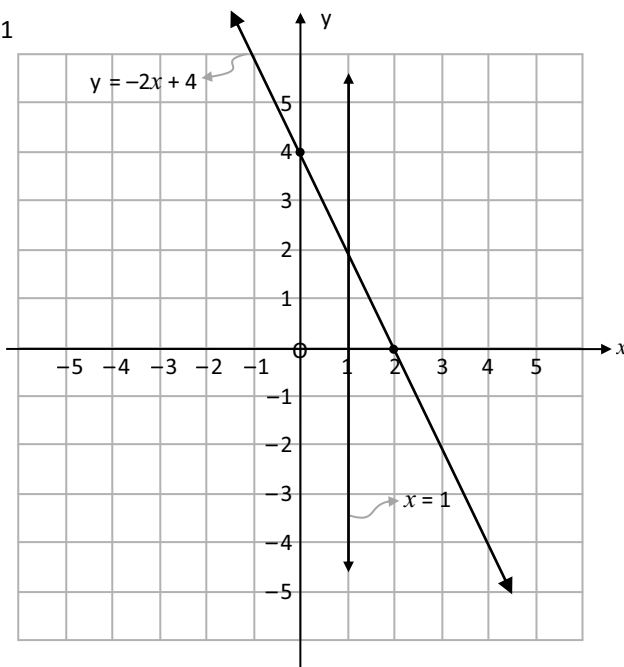
Interessantheidshalwe:

Vergelyk die gradiënte, $-\frac{2}{3}$ en $\frac{3}{2}$.

Hulle is negatiewe inverses van mekaar.



11.1



Om die punte te bepaal waar die grafieke die asse sny:

$$y = -2x + 4:$$

y-afsnit (stel $x = 0$ in): $y = -2(0) + 4$
 $= 4$

x-afsnit (stel $y = 0$ in): $0 = -2x + 4$
 $\therefore 2x = 4$
 $\therefore x = 2$

$x = 1$: Hierdie grafiek is 'n **vertikale** lyn deur $x = 1$.
Elke punt op die grafiek het 'n x -koordinaat gelyk aan 1.

11.2 Die snypunt is (1; 2) ◀

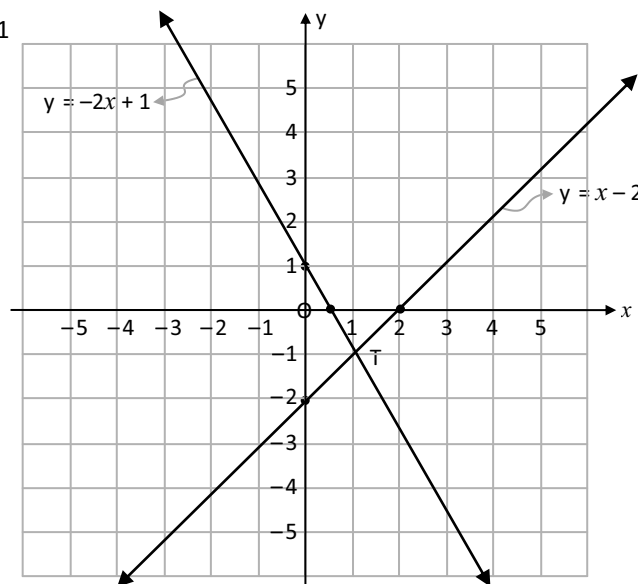
... By hierdie punt, $x = 1$ en $y = -2x + 4$
(d.w.s. albei vergelykings is waar)

$$\therefore y = -2(1) + 4$$

$$= 2$$

$\therefore$ Die punt is (1; 2)

12.1



Om die punte te bepaal waar die grafieke die asse sny:

$$y = -2x + 1:$$

Vir die **Y-afsnit**, stel $x = 0$ in

$$\therefore y = -2(0) + 1$$

$$= 1$$

$\therefore$ Die grafiek sny die **y-as** by 1.

Die **punt** is (0; 1)

Vir die **X-afsnit**, stel $y = 0$ in

$$\therefore 0 = -2x + 1$$

$$\therefore 2x = 1$$

$$\therefore x = \frac{1}{2}$$

$\therefore$ Die grafiek sny die **x-as** by $\frac{1}{2}$.

Die **punt** is $(\frac{1}{2}; 0)$

$$y = x - 2:$$

$$\therefore y = (0) - 2$$

$$= -2$$

$\therefore$ Die grafiek sny die **y-as** by -2.

Die **punt** is (0; -2)

$$\therefore 0 = x - 2$$

$$\therefore x = 2$$

$\therefore$ Die grafiek sny die **x-as** by 2.

Die **punt** is (2; 0)

12.2 $y = -2x + 1 \dots \textcircled{1}$ & $y = x - 2 \dots \textcircled{2}$

$$\textcircled{1} = \textcircled{2}: -2x + 1 = x - 2$$

$$\therefore -2x - x = -2 - 1$$

$$\therefore -3x = -3$$

$$\therefore x = 1$$

Albei vergelykings moet waar wees by T, die snypunt.



Stel $x = 1$ in, in $\textcircled{2}$: $y = (1) - 2$ [OF in $\textcircled{1}$!]

$$= -1$$

$$\therefore T(1; -1) \blacktriangleleft$$

NOTAS

